

	COLEGIO ITALICA Arguijo 5-7 SEVILLA 41003	MATEMATICAS 4º ESO EVAL: 1ª FECHA: 18-11-16	
NOMBRE			

a) $x^4 - 10x^3 + 5x^2 + 40x - 36 = 0$

$$\begin{array}{c|ccccc} 1 & 1 & -10 & 5 & 40 & -36 \\ \hline 1 & & 1 & -9 & -4 & 36 \\ \hline & 1 & -9 & -4 & 36 & \boxed{0} \end{array}$$

$$\begin{array}{c|cccc} 2 & 1 & -9 & -4 & 36 \\ \hline 2 & & 2 & -14 & -36 \\ \hline & 1 & -7 & -18 & \boxed{0} \end{array}$$

$$(x-1)(x^3 - 9x^2 - 4x + 36) = 0 \quad (x-1)(x-2)(x^2 - 7x - 18) = 0$$

$$x-1=0 \rightarrow \boxed{x=1}$$

$$x-2=0 \rightarrow \boxed{x=2}$$

$$x^2 - 7x - 18 = 0 \rightarrow x = \frac{7 \pm \sqrt{49 + 72}}{2} = \frac{7 \pm 11}{2} = \begin{cases} \boxed{x=9} \\ \boxed{x=-2} \end{cases}$$

b) $\frac{x+1}{x^2 - 2x} + \frac{x-1}{x} = 2$

$$\frac{x+1}{x(x-2)} + \frac{x-1}{x} = 2 \rightarrow \frac{x+1}{\cancel{x(x-2)}} + \frac{(x-1)(x-2)}{\cancel{x(x-2)}} = \frac{2x(x-2)}{\cancel{x(x-2)}}$$

$$x+1 + x^2 - 2x - x + 2 = 2x^2 - 4x$$

$$x^2 - 2x - 3 = 0$$

$$x = \frac{2 \pm \sqrt{4+12}}{2} = \frac{2 \pm 4}{2} = \begin{cases} \boxed{x=3} \\ \boxed{x=-1} \end{cases}$$

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$$c) \sqrt{13-x^2} + x = 5$$

$$\left(\sqrt{13-x^2}\right)^2 = (5-x)^2 \rightarrow 13-x^2 = 25+x^2-10x$$

$$2x^2 - 10x + 12 = 0 \rightarrow x^2 - 5x + 6 = 0$$

$$x = \frac{5 \pm \sqrt{25-24}}{2} = \frac{5 \pm 1}{2} = \begin{cases} \boxed{x=3} & \sqrt{13-9} + 3 = 5 \rightarrow 2+3=5 \quad v \\ \boxed{x=2} & \sqrt{13-4} + 2 = 5 \rightarrow 3+2=5 \quad v \end{cases}$$

$$d) x^4 - 13x^2 + 36 = 0$$

$$\boxed{x^2 = y} \rightarrow y^2 - 13y + 36 = 0$$

$$y = \frac{13 \pm \sqrt{169-144}}{2} = \frac{13 \pm 5}{2} = \begin{cases} y=9 \rightarrow \boxed{x=\pm 3} \\ y=4 \rightarrow \boxed{x=\pm 2} \end{cases}$$

$$e) \frac{x+7}{x+3} + \frac{x^2-3x+6}{x^2+2x-3} = 1$$

$$\frac{x+7}{x+3} + \frac{x^2-3x+6}{(x+3)(x-1)} = 1 \rightarrow \frac{(x+7)(x-1)}{\cancel{(x+3)(x-1)}} + \frac{x^2-3x+6}{\cancel{(x+3)(x-1)}} = \frac{(x+3)(x-1)}{\cancel{(x+3)(x-1)}}$$

$$x^2 - x + 7x - 7 + x^2 - 3x + 6 = x^2 - x + 3x - 3$$

$$x^2 + x + 2 = 0$$

$$x = \frac{-1 \pm \sqrt{1-8}}{2} \notin \mathbb{R}$$